

e^+e^- Dijet Event Shapes

Carola F. Berger

EPS 2003

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based on

C.F.B., T. Kúcs, G. Stermán, arXiv:hep-ph/0212343.

G. Stermán, arXiv:hep-ph/0301243.

C.F.B., T. Kúcs, G. Stermán, Phys. Rev. **D 68** (2003) [arXiv:hep-ph/0303051].

C.F.B., arXiv:hep-ph/0305076.

and in preparation.

Outline

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- Introduction, General Class of e^+e^- Event Shapes

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- Summary and Outlook

Introduction - e^+e^- Event Shapes

Thrust

E. Farhi, Phys. Rev. Lett. **39**, 1587 (1977).

$$T = \frac{1}{\sum_j |\vec{p}_j|} \max_{\hat{n}} \sum_{i=1}^n |\vec{p}_i \cdot \hat{n}| = \frac{1}{\sum_j |\vec{p}_j|} \max_{\hat{n}} \sum_i k_{\perp,i} e^{-|\eta_i|} \quad (1)$$

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Jet broadening

S. Catani, G. Turnock, B. R. Webber, Phys. Lett. **B 295**, 269 (1992).

$$B = \frac{1}{\sum_j |\vec{p}_j|} \sum_{i=1}^n |k_{\perp,i}| \quad (2)$$

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Generalization:

C.F.B., T. Kúcs, G. Sterman, arXiv:hep-ph/0212343, and Phys. Rev. D **68** (2003),

arXiv:hep-ph/0303051; A. Banfi, G. P. Salam and G. Zanderighi, arXiv:hep-ph/0304148.

$$\tau_a(N) = \frac{1}{Q} \sum_{\text{all } i \in N} k_{\perp,i} e^{-|\eta_i|(1-a)} \quad (3)$$

Parameter a allows to control shape. $a = 0 : 1 - T$, $a = 1 : B$.

Generalized Event Shapes - Resummation

Cross section $e^+e^- \rightarrow 2\text{Jets}$, c.m. energy Q :

$$\frac{d\sigma(\tau_a, Q)}{d\tau_a} = \frac{1}{2Q^2} \sum_N |M(N)|^2 \delta(\tau_a - \tau_a(N)). \quad (4)$$

$0 < \tau_a \ll 1$ in 2-jet limit \Rightarrow **large logarithmic corrections** $\sim \ln \tau_a$

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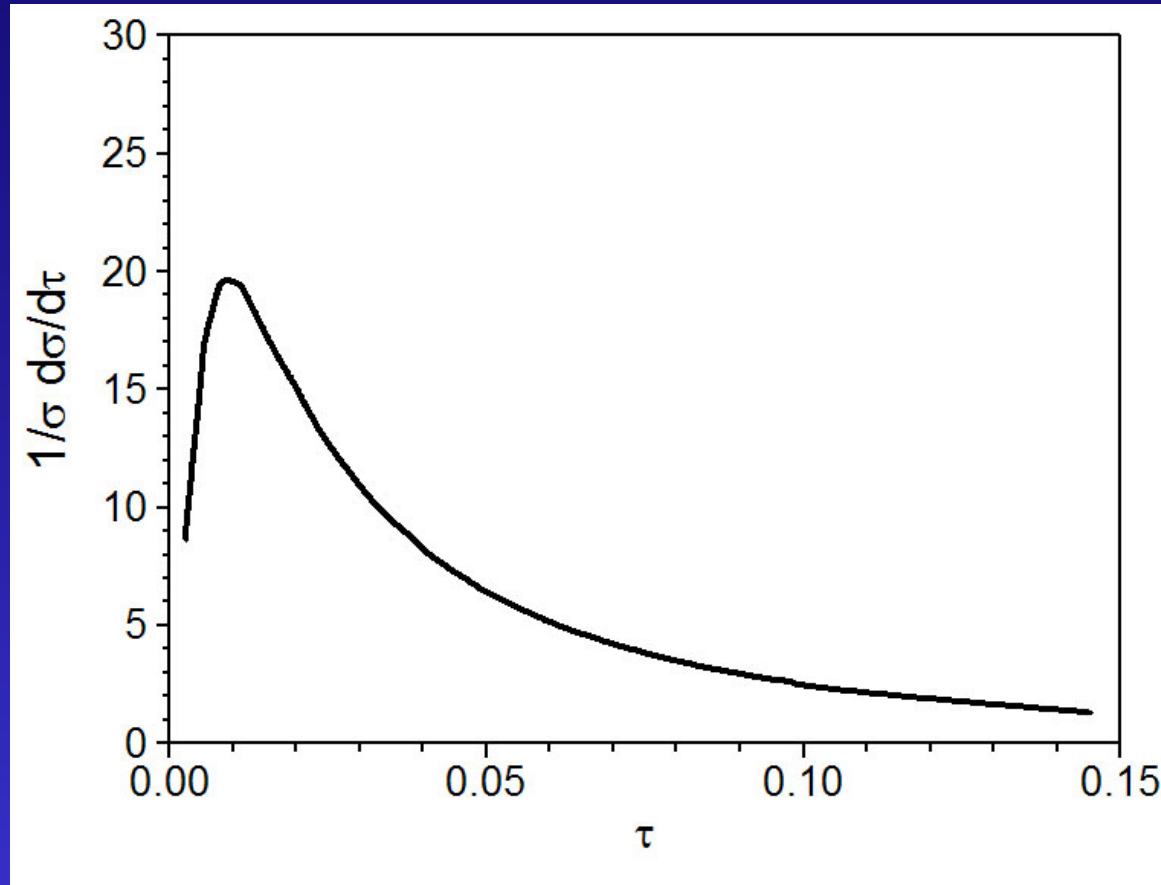
Resummed cross section in Laplace transform space: 7

C.F.B., T. Kúcs, G. Sterman, *Phys. Rev. D* 68 (2003), arXiv:hep-ph/0303051.

$$\frac{1}{\sigma_{\text{tot}}} \tilde{\sigma}(\nu, Q, a) \equiv \frac{1}{\sigma_{\text{tot}}} \int_0^1 d\tau_a e^{-\nu \tau_a} \frac{d\sigma(\tau_a, Q)}{d\tau_a} \quad (5)$$

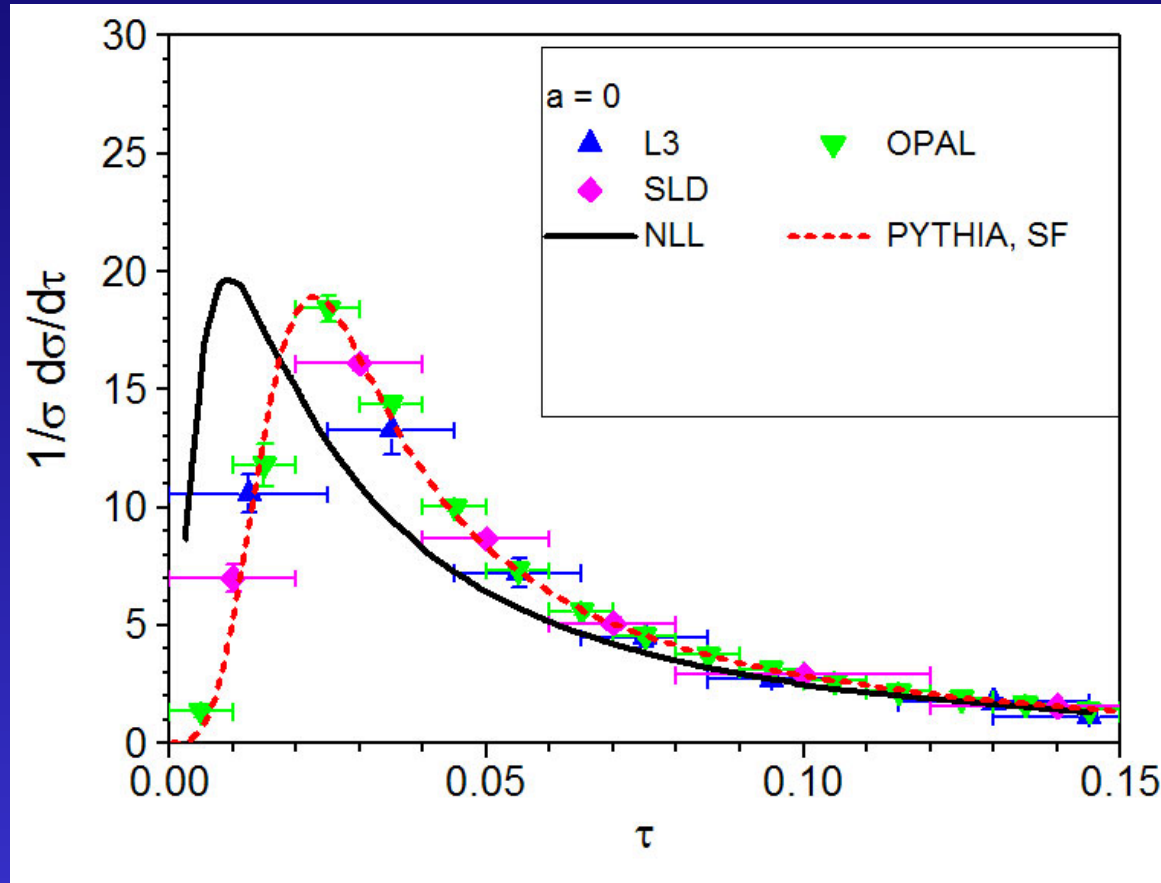
$$= \exp \left\{ 2 \int_0^1 \frac{du}{u} \left[\int_{u^2 Q^2}^{uQ^2} \frac{dp_{\perp}^2}{p_{\perp}^2} A(\alpha_s(p_{\perp})) \left(e^{-u^{1-a} \nu (p_{\perp}/Q)^a} - 1 \right) + \frac{1}{2} B(\alpha_s(\sqrt{u}Q)) \left(e^{-u(\nu/2)^{2/(2-a)}} - 1 \right) \right] \right\}. \quad (6)$$

NLL Resummed Cross Section vs. Data at $Q = 91 \text{ GeV}$



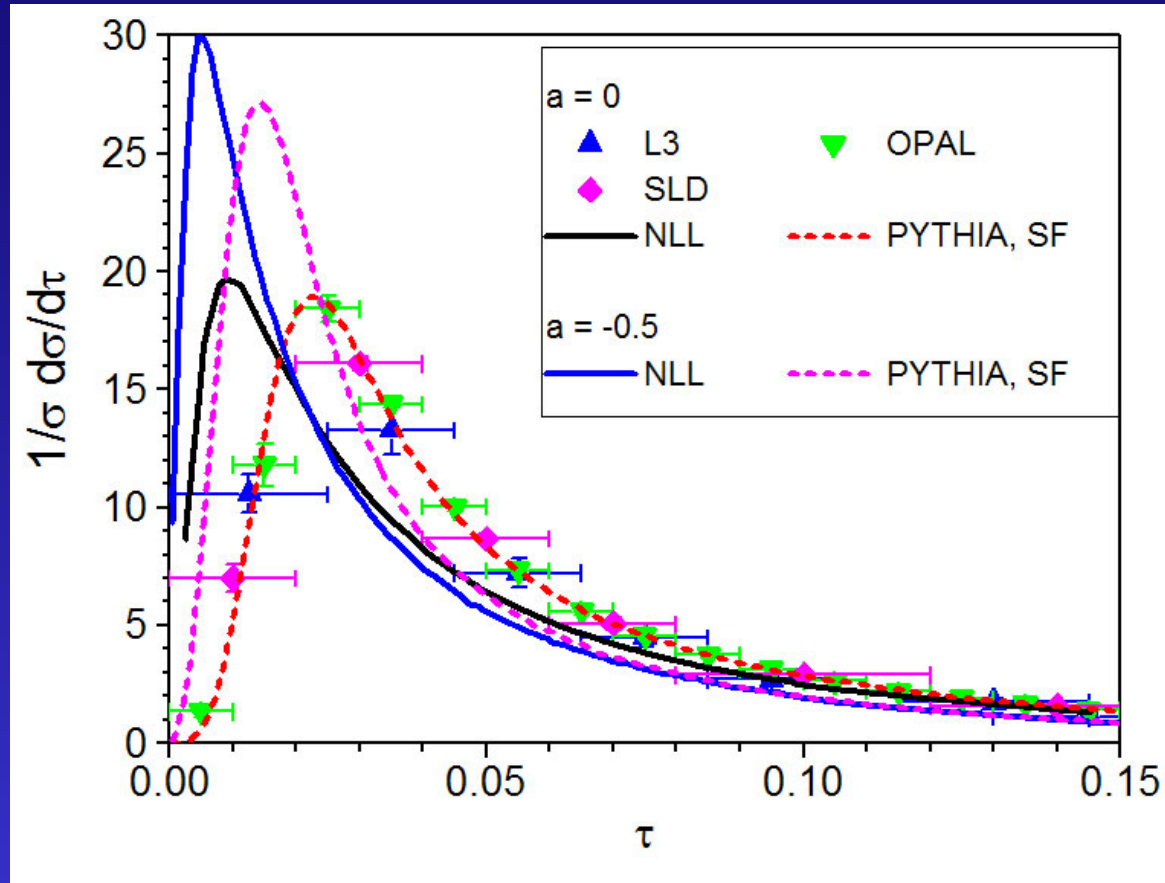
Thrust-data: L3, Z. Phys. **C 55**, 39 (1992). OPAL, Z. Phys. **C 59**, 1 (1993). SLD, Phys. Rev. **D 51**, 962 (1995). PYTHIA v. 6.215: T. Sjostrand, P. Eden, C. Friberg, L. Lonnblad, G. Miu, S. Mrenna and E. Norrbin, Comput. Phys. Commun. **135**, 238 (2001) [arXiv:hep-ph/0010017].

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Nonperturbative Corrections

Rewrite (6):

$$\begin{aligned}
 \ln \left[\frac{1}{\sigma_{\text{tot}}} \tilde{\sigma}(\nu, Q, a) \right] &= 2 \left[\int_0^{\kappa^2} \frac{dp_{\perp}^2}{p_{\perp}^2} + \int_{\kappa^2}^{Q^2} \frac{dp_{\perp}^2}{p_{\perp}^2} \right] A(\alpha_s(p_{\perp})) \int_{p_{\perp}^2/Q^2}^{p_{\perp}/Q} \frac{du}{u} \left(e^{-u^{1-a} \nu (p_{\perp}/Q)^a} - 1 \right) \\
 &+ \left[\int_0^{\kappa^2/Q^2} \frac{du}{u} + \int_{\kappa^2/Q^2}^{Q^2} \frac{du}{u} \right] B(\alpha_s(\sqrt{u}Q)) \left(e^{-u(\nu/2)^{2/(2-a)}} - 1 \right) \\
 &\equiv \ln \left[\frac{1}{\sigma_{\text{tot}}} \tilde{\sigma}_{\text{PT}}(\nu, Q, \kappa, a) \right] \\
 &+ \frac{\mathbf{2}}{\mathbf{1-a}} \sum_{n=1}^{\infty} \frac{1}{n n!} \left(-\frac{\nu}{Q} \right)^n \int_0^{\kappa^2} \frac{dp_{\perp}^2}{p_{\perp}^2} p_{\perp}^n A(\alpha_s(p_{\perp})) \\
 &+ \mathcal{O} \left(\frac{\nu}{Q^{2-a}}, \frac{\nu^{2-a}}{Q^2} \right). \tag{7}
 \end{aligned}$$

G. P. Korchemsky, arXiv:hep-ph/9806537; G. P. Korchemsky and G. Sterman, Nucl. Phys. B **555**, 335 (1999) [arXiv:hep-ph/9902341].

Nonperturbative Corrections - Shape Function

$$\ln \left[\frac{1}{\sigma_{\text{tot}}} \tilde{\sigma}(\nu, Q, a) \right] \equiv \ln \left[\frac{1}{\sigma_{\text{tot}}} \tilde{\sigma}_{\text{PT}}(\nu, Q, \kappa, a) \right] + \ln \tilde{f}_{a,\text{NP}} \left(\frac{\nu}{Q}, \kappa \right), \quad (8)$$

$$\ln \tilde{f}_{a,\text{NP}} \left(\frac{\nu}{Q}, \kappa \right) \equiv \frac{\mathbf{1}}{\mathbf{1} - \mathbf{a}} \sum_{n=1}^{\infty} \lambda_n(\kappa) \left(-\frac{\nu}{Q} \right)^n. \quad (9)$$

G. Sterman, arXiv:hep-ph/0301243.

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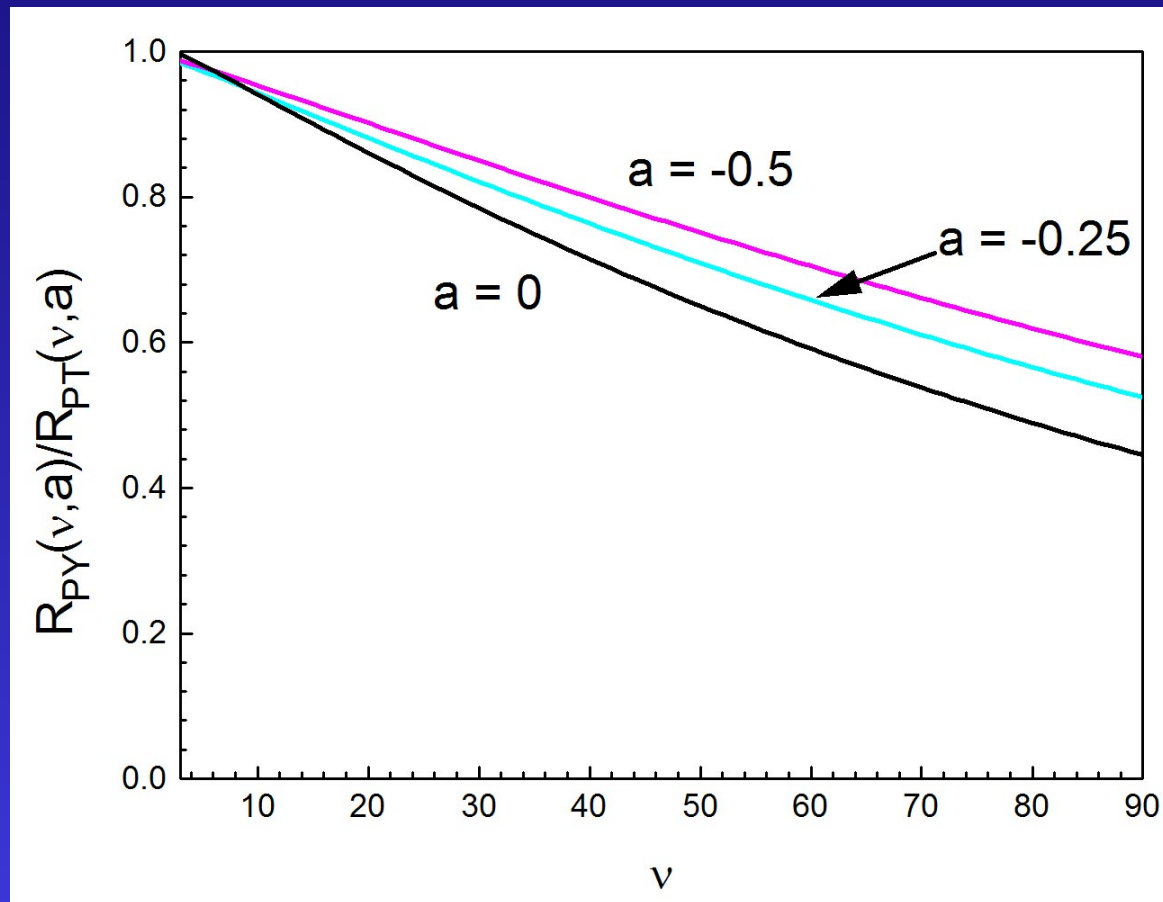
⇒ **Scaling rule for shape function:**

$$\tilde{f}_{a,\text{NP}} \left(\frac{\nu}{Q}, \kappa \right) = \frac{\tilde{\sigma}(\nu, Q, a)}{\tilde{\sigma}_{\text{PT}}(\nu, Q, \kappa, a)} + \mathcal{O} \left(\frac{1}{Q^{1-a}} \right) \quad (10)$$

$$\tilde{f}_{a,\text{NP}} \left(\frac{\nu}{Q}, \kappa \right) = \left[\tilde{f}_{0,\text{NP}} \left(\frac{\nu}{Q}, \kappa \right) \right]^{\frac{1}{1-a}} \quad (11)$$

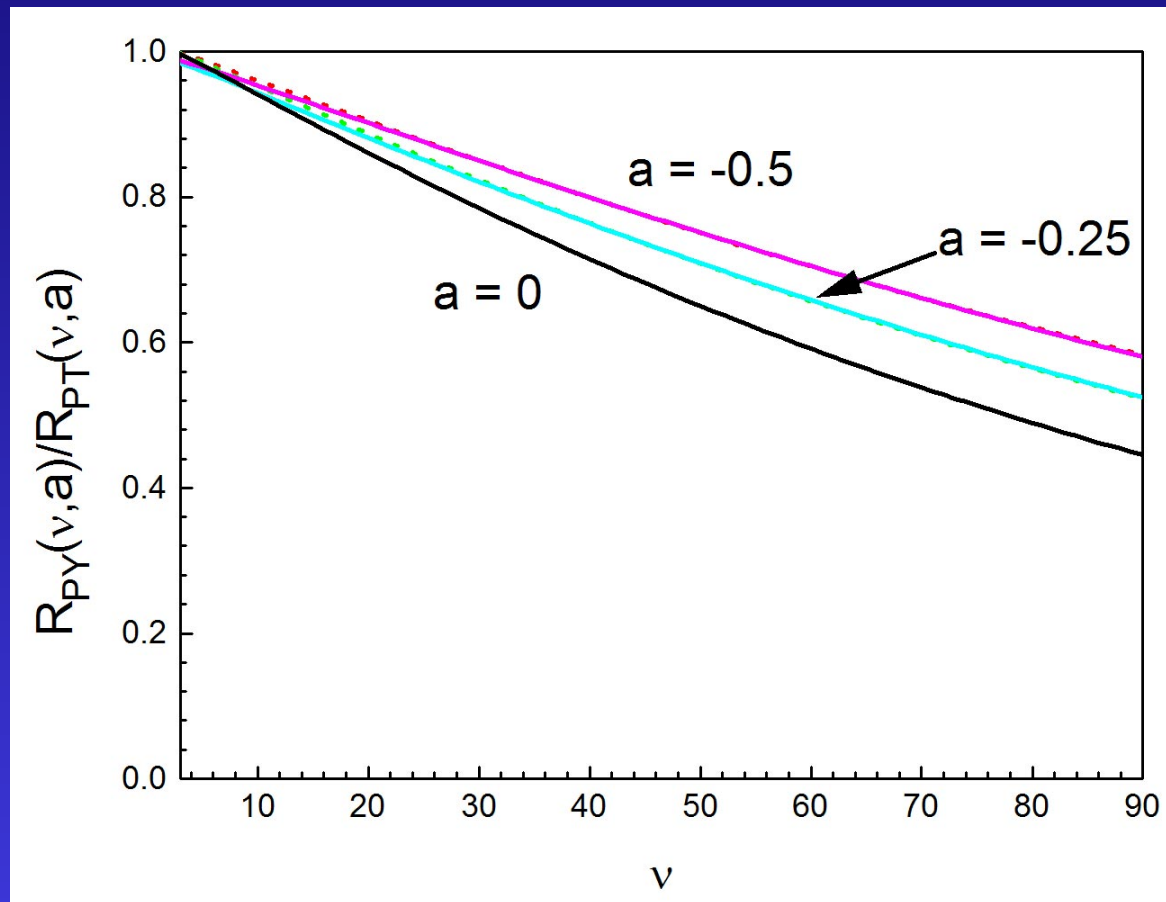
Nonperturbative Corrections - Tests of Scaling

$\tilde{f}_{a, \text{NP}}\left(\frac{\nu}{Q}\right)$ at $Q = 91$ GeV (PYTHIA/NLL),
directly computed



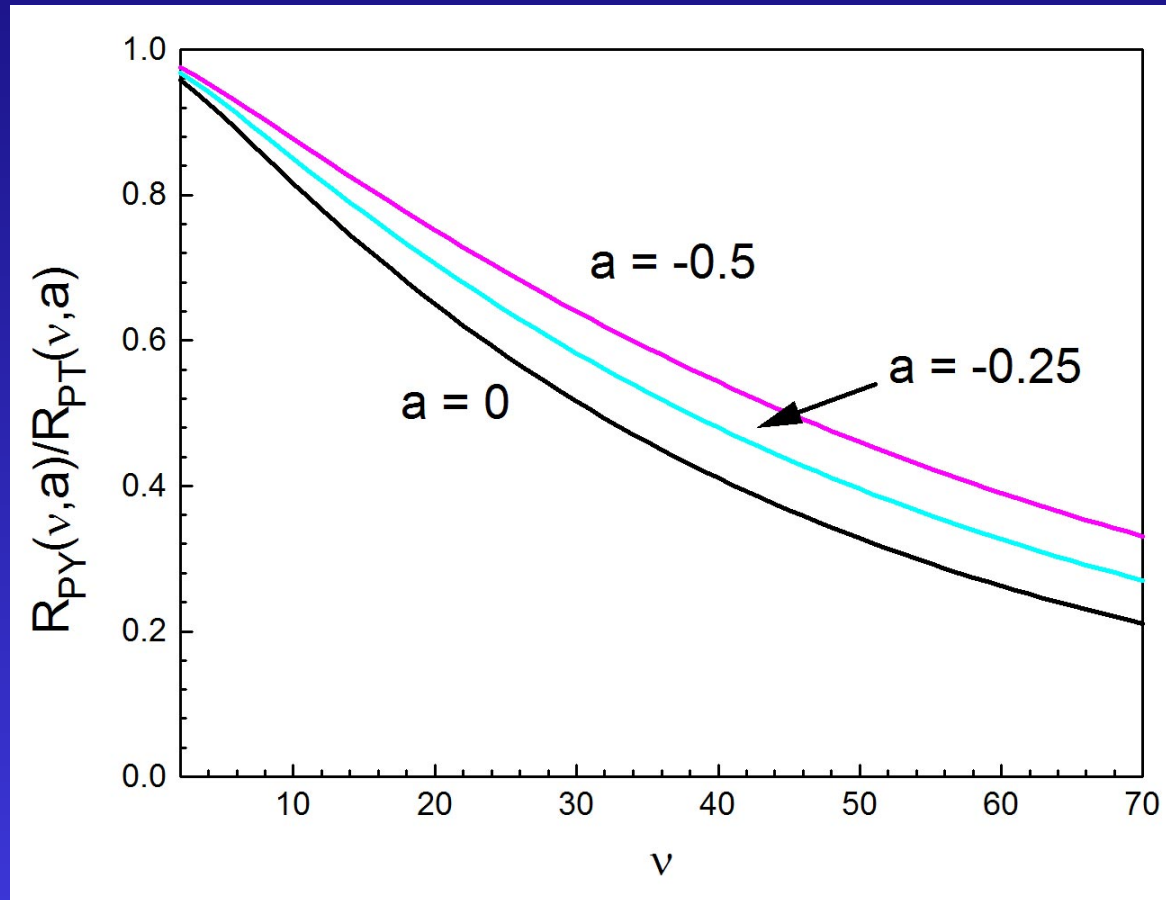
Nonperturbative Corrections - Tests of Scaling

$\tilde{f}_{a,\text{NP}}\left(\frac{\nu}{Q}\right)$ at $Q = 91$ GeV (PYTHIA/NLL),
directly computed vs. **prediction from scaling**



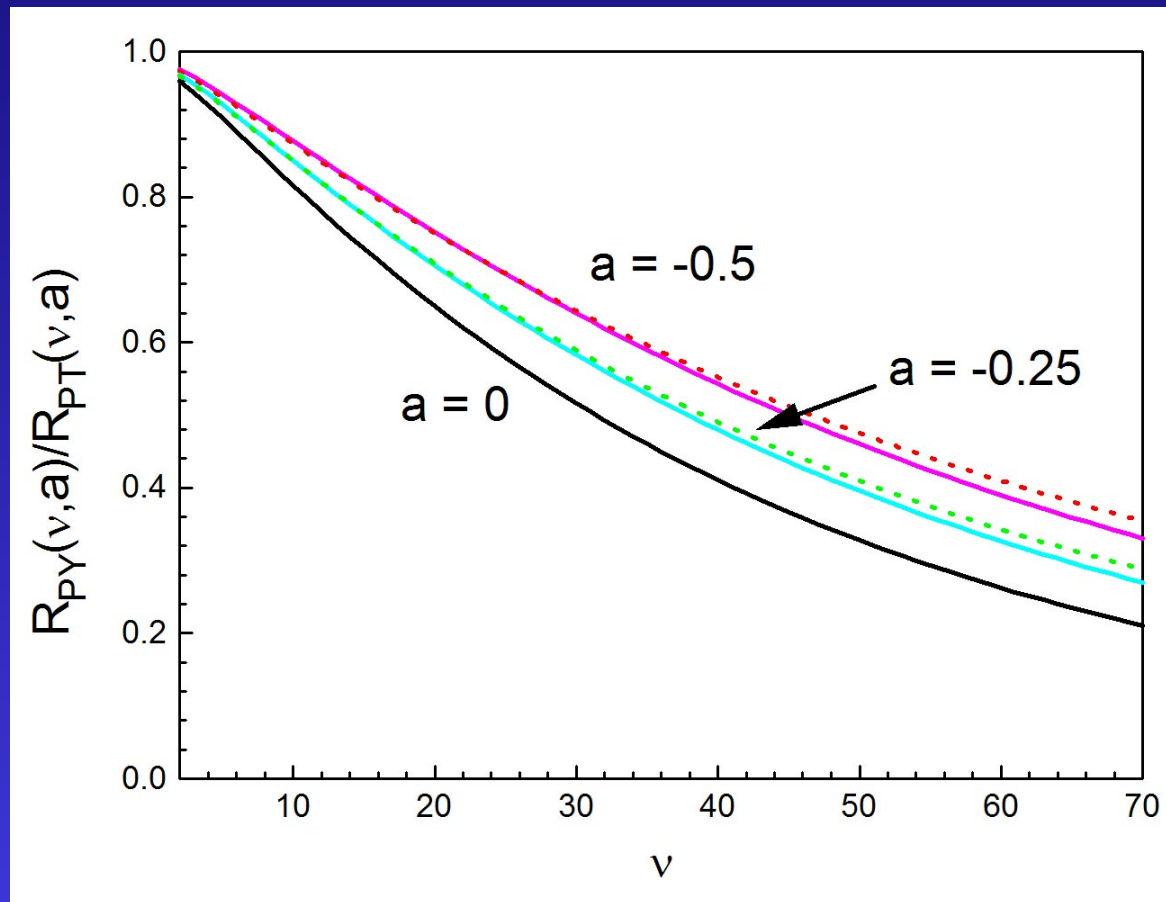
Nonperturbative Corrections - Tests of Scaling

$\tilde{f}_{a,\text{NP}}\left(\frac{\nu}{Q}\right)$ at $Q = 35$ GeV (PYTHIA/NLL),
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Scaling \Rightarrow

✓ universality of power corrections within general class

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- \rightarrow predictions in momentum space
- \rightarrow extension of resummation to $a \approx 1$ - inclusion of recoil Y. L. Dokshitzer, A. Lucenti, G. Marchesini and G. P. Salam, JHEP **9801**, 011 (1998) [arXiv:hep-ph/9801324].