

# Testing BFKL using high- $t$ vector meson production

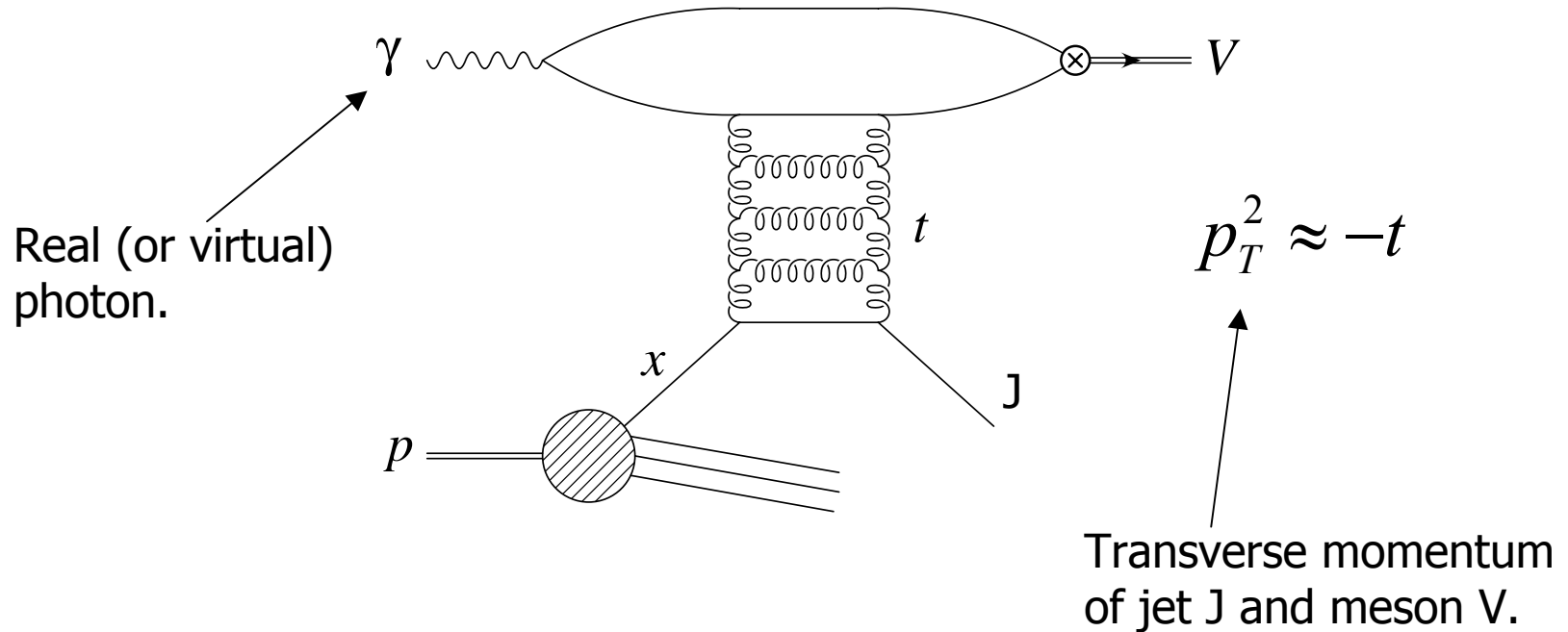
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# High-t Meson Production



$$xW^2 \gg -t \gg \Lambda^2$$

There is a **rapidity gap** between the meson V and the jet, J.

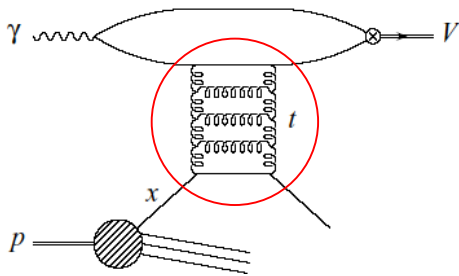
# Motivation

- ✓ Large momentum transfer: an excellent opportunity to elucidate our understanding of **rapidity gap processes in a perturbative environment**.
- ✓ No need to measure the dissociating proton: obvious experimental advantage; can reach **high rapidity gaps** (<6 units) and therefore probe QCD in a region where fixed order PT breaks down (**BFKL**).
- ✓ Relatively rare, means we are only recently getting **high quality data** from HERA.
- ✓ No “gap survival” problems. Variety of mesons to measure (and photons).

# Lowest order BFKL

Asymptotically:

$$\frac{d\sigma}{dt}(\gamma q \rightarrow Vq) \sim \frac{\alpha_s^4}{t^4} \left( \frac{s}{s_0} \right)^{2\omega_0}$$



$$\omega_0 = 12 \ln 2 \frac{\alpha_s}{\pi}$$

Regge cut

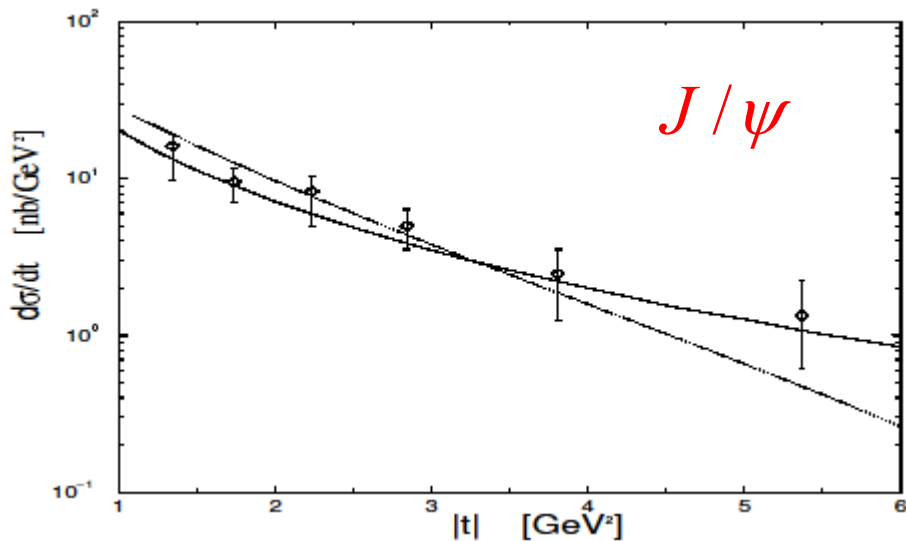
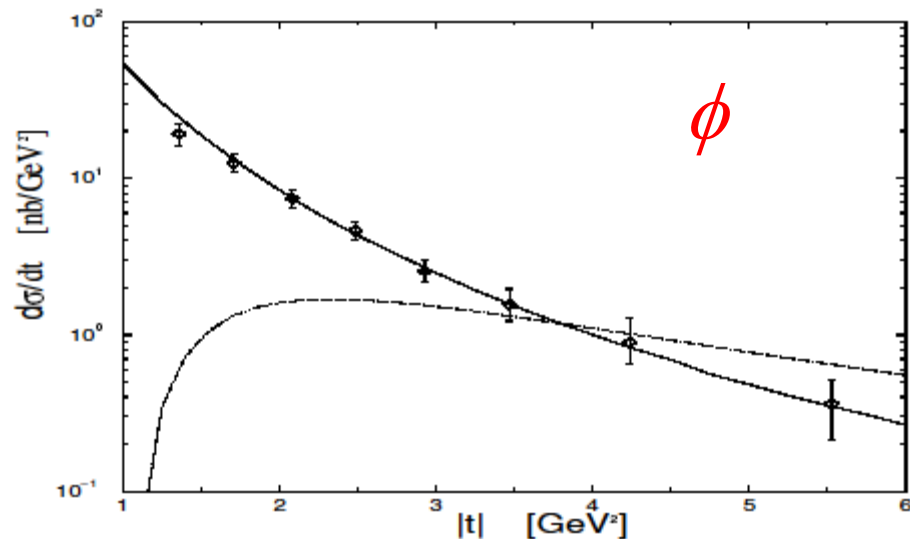
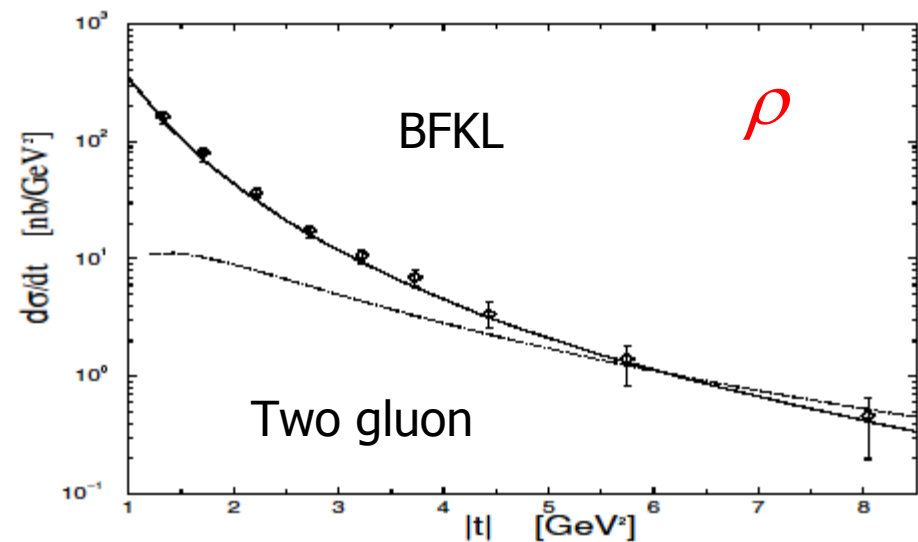
BFKL = summing logarithms in energy:

$$\sum_n \left( c_n^0 \alpha_s^n \ln^n(s/s_0) + c_n^1 \alpha_s^n \ln^{n-1}(s/s_0) + \dots \right)$$

LL

- ✓ Complete LL calculations do go beyond the asymptotic approximation
- ✓ But they treat the vector meson in a non-relativistic limit i.e. the quark and antiquark have no relative transverse momentum and share equally the meson's longitudinal momentum.
- ✓ And they keep only lowest conformal spin "n=0" (BFKL amplitude can be written as a sum over functions labelled by the way they transform under the conformal group, n=0 dominates at large enough centre-of-mass energy)
- ✓ Even so, LL seems to work very well indeed...

# Comparison to ZEUS data



✗ LO BFKL works remarkably well:  
Three parameter fit

$$\alpha_s \text{ and } s_0 = \beta M_V^2 - \gamma t$$

Fit prefers

$$\alpha_s \approx 0.20 \text{ and } s_0 \approx M_V^2$$

✗ Two-gluon exchange fails

# Fixed order perturbation theory

- ✓ Two-gluon exchange calculations (and fixed order calculations in general) miss some essential physics They predict that one gluon should carry all the momentum transfer whilst the other carries none

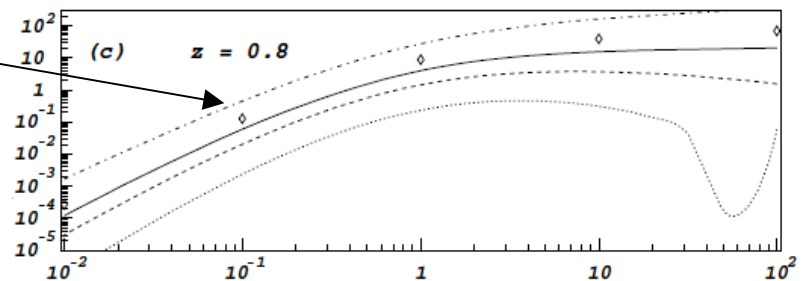
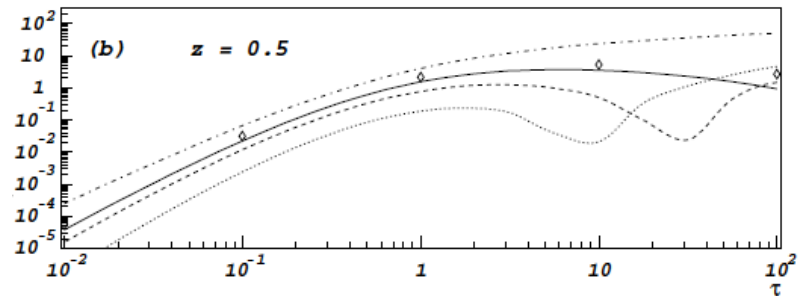
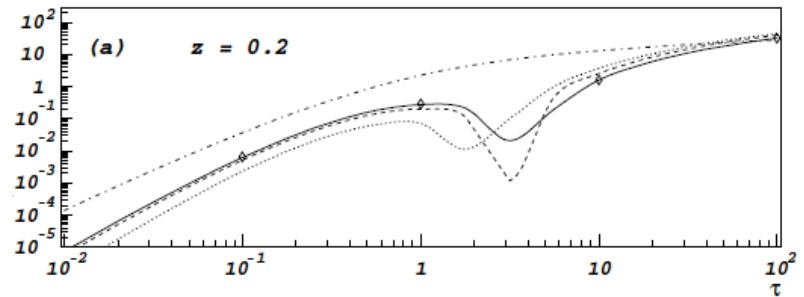
- ✓ Need to resum double logs:

$$\exp[ \sim \alpha_s \ln(k^2 (k - q)^2 / q^2) \ln s ]$$

- ✓ And also single logs:

$$\sim \alpha_s \ln s$$

Poor convergence of perturbation series (even after resumming double logs – it is much worse if one does not resum them )



# Improving the original calculations I: Relativistic Corrections

- ✓ Original calculations of D.Ivanov et al implement full lightcone wavefunctions of the vector mesons but in a two-gluon exchange model

Two-gluon exchange is IR divergent due to endpoint singularities in the integral over the quark/antiquark momentum fractions. This divergence is not present after BFKL summation.

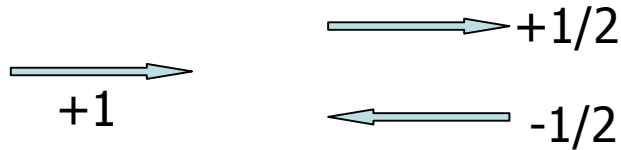
- ✓ For light mesons naïvely expect “chiral even” term to dominate

Ivanov et al argued that although the chiral even term dominates at asymptotically high momentum transfers, there should be a significant chiral odd component at HERA energies.



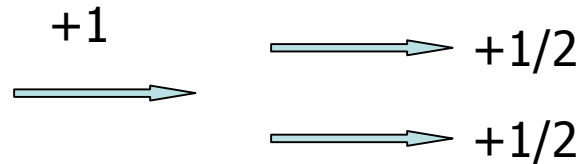
## Chiral Even

Naively expect light mesons to be predominantly **longitudinal**



But longitudinal amplitude should vanish if the quark and antiquark are collinear and share equally the meson's momentum

## Chiral Odd



Expect meson to be predominantly **same helicity** as photon

} HERA data

But the amplitude should be suppressed by  $m^2 / |t|$

↑  
Condensate? Current mass? Constituent mass?

( Nb: Chiral odd is the only contribution in the non-relativistic approximation used in the original calculations. )

Closed analytic expressions have now been obtained for all amplitudes:

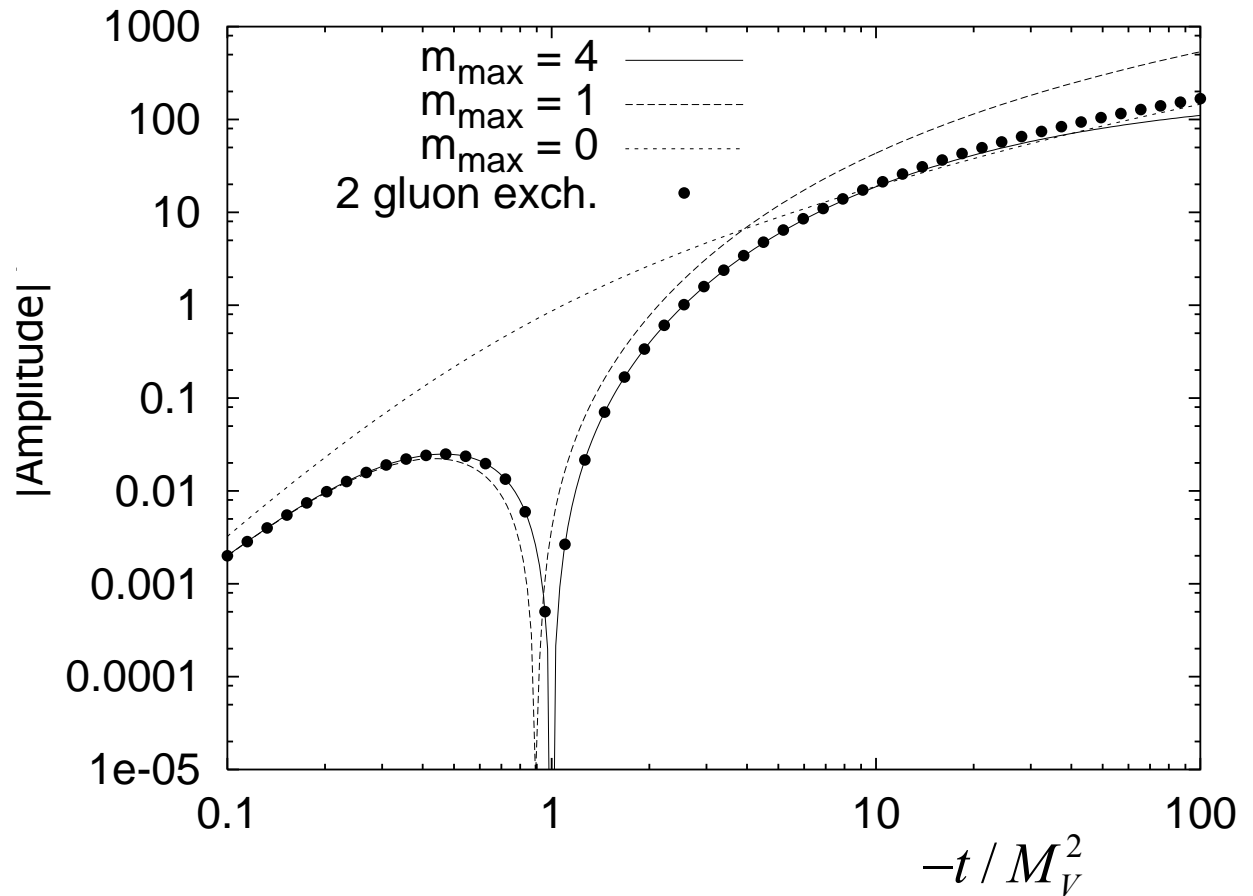
$$M_{++}^{\text{odd}} = \frac{C_V f_V^T}{4|q|} \int_0^1 du 6u(1-u) \\ \times \sum_{n=-\infty}^{n=+\infty} \int_{-\infty}^{\infty} d\nu \frac{\nu^2 + n^2}{[\nu^2 + (n - 1/2)^2][\nu^2 + (n + 1/2)^2]} \frac{\exp[\chi_{2n}(\nu)z]}{\sin(i\pi\nu)} I_{-\frac{1}{2}-\frac{1}{2}}(\nu, 2n, q, u; 0)$$

$$I_{\alpha\beta}(\nu, n, q, u; a) = -\frac{m}{2} \int_{C'-i\infty}^{C'+i\infty} \frac{d\zeta}{2\pi i} \Gamma(a/2 - \zeta) \Gamma(-a/2 - \zeta) \tau_q^\zeta (i \operatorname{sign}(2u - 1))^{\alpha - \beta + n} \\ \times \left( \frac{4}{|q|} \right)^4 [\sin \pi(\alpha + \mu + \zeta) B(\alpha, \mu, q^*, u, \zeta) B(\beta, \tilde{\mu}, q, u^*, \zeta) \\ - (-1)^n \sin \pi(\alpha - \mu + \zeta) B(\alpha, -\mu, q^*, u, \zeta) B(\beta, -\tilde{\mu}, q, u^*, \zeta) ]$$

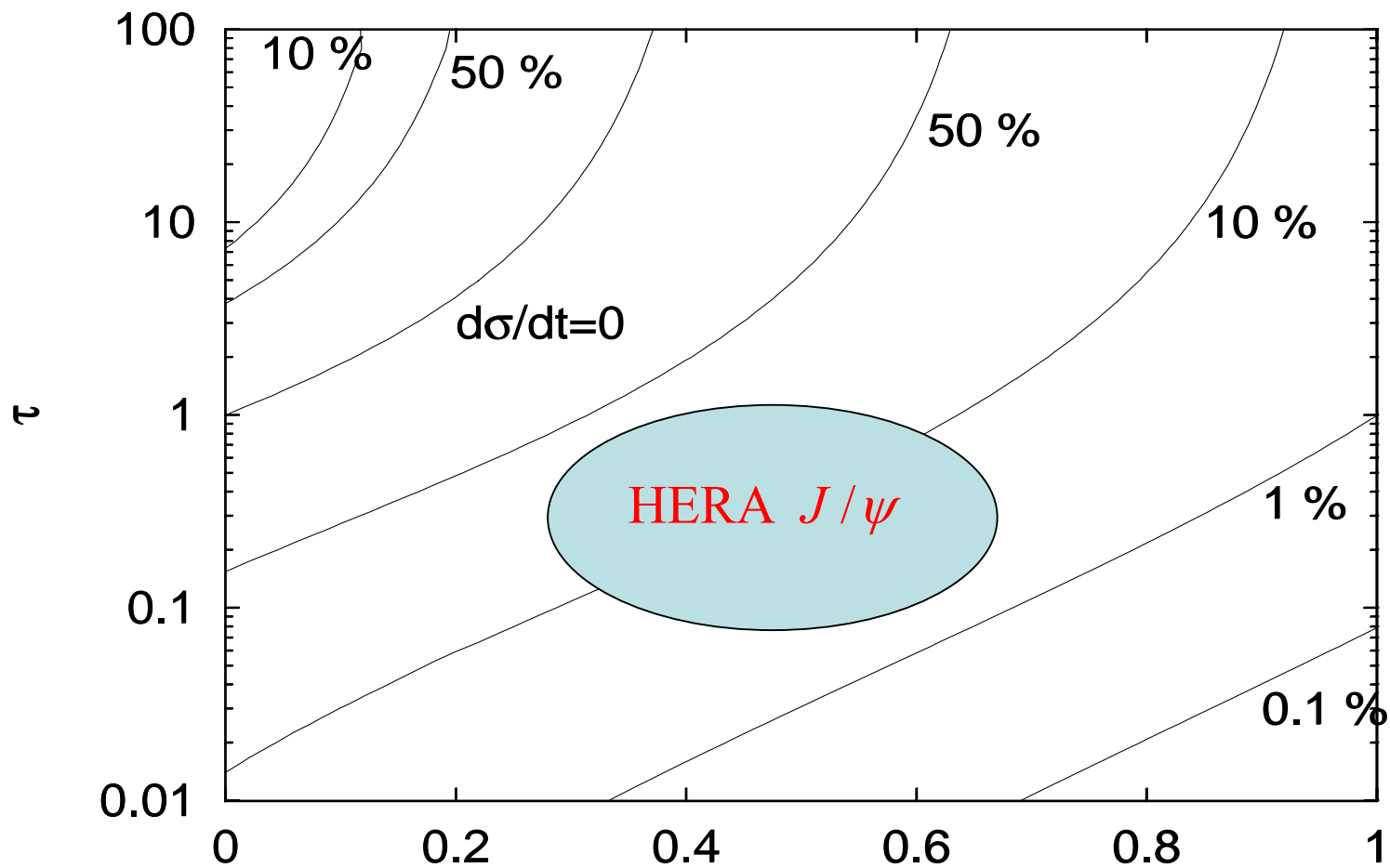
$$B(\alpha, \mu, q^*, u, \zeta) = (-4u\bar{u})^{-(\mu+2+\alpha+\zeta)/2} \left( \frac{4}{q^*} \right)^\alpha 2^{-\mu} \frac{\Gamma(\mu + 2 + \alpha + \zeta)}{\Gamma(\mu + 1)} \\ {}_2F_1 \left( \frac{\mu + 2 + \alpha + \zeta}{2}, \frac{\mu - 1 - \alpha - \zeta}{2}; \mu + 1; \frac{1}{4u\bar{u}} \right).$$

# Improving the original calculations II: Conformal Spin

Higher conformal spin is **necessary** to match BFKL to the two-gluon approximation at zero rapidity.



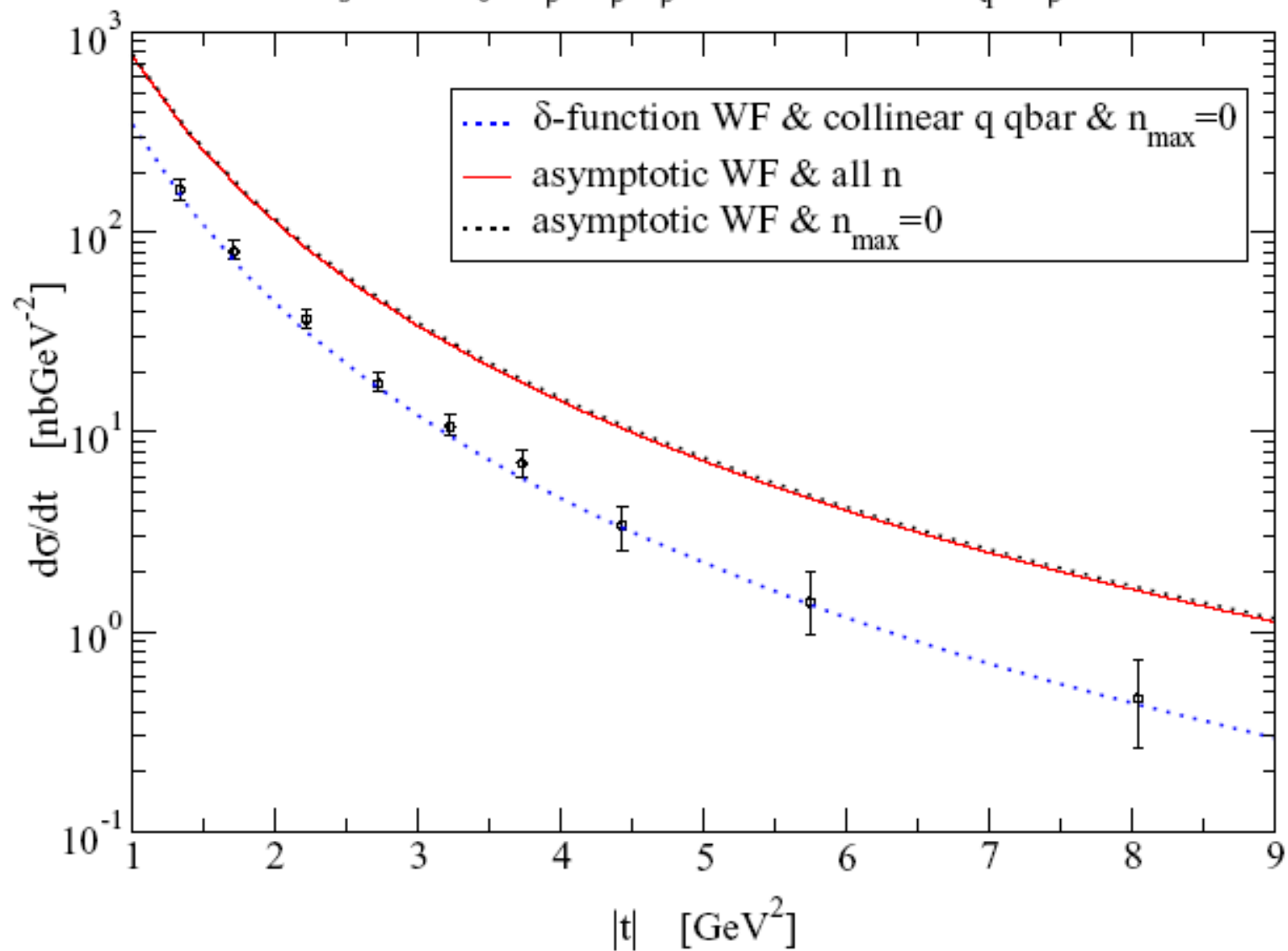
# Higher conformal spin is a modest effect at HERA



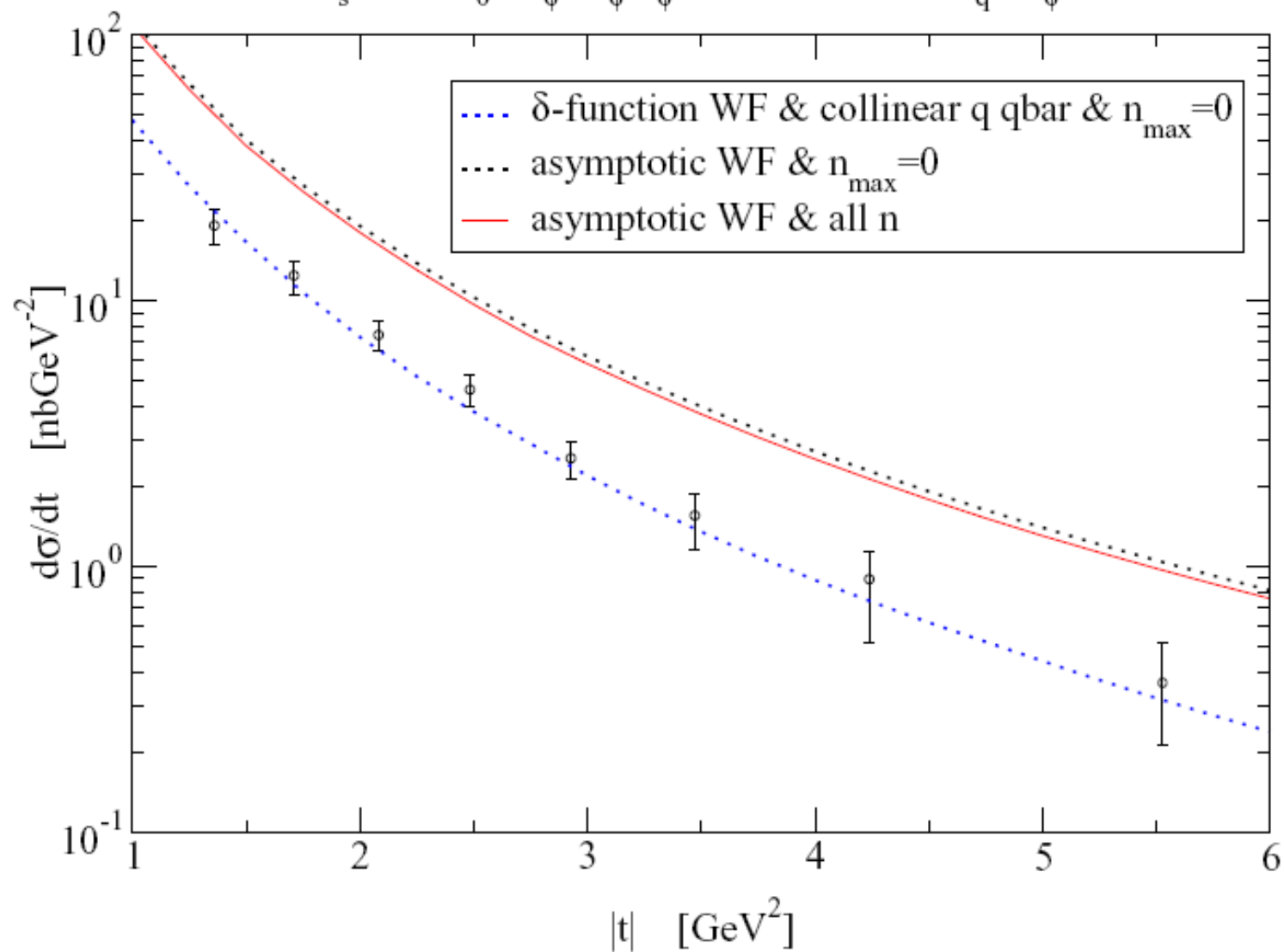
Contours of fixed

$$\frac{|\sigma(\text{all } n) - \sigma(n = 0)|}{\sigma(n = 0)}$$

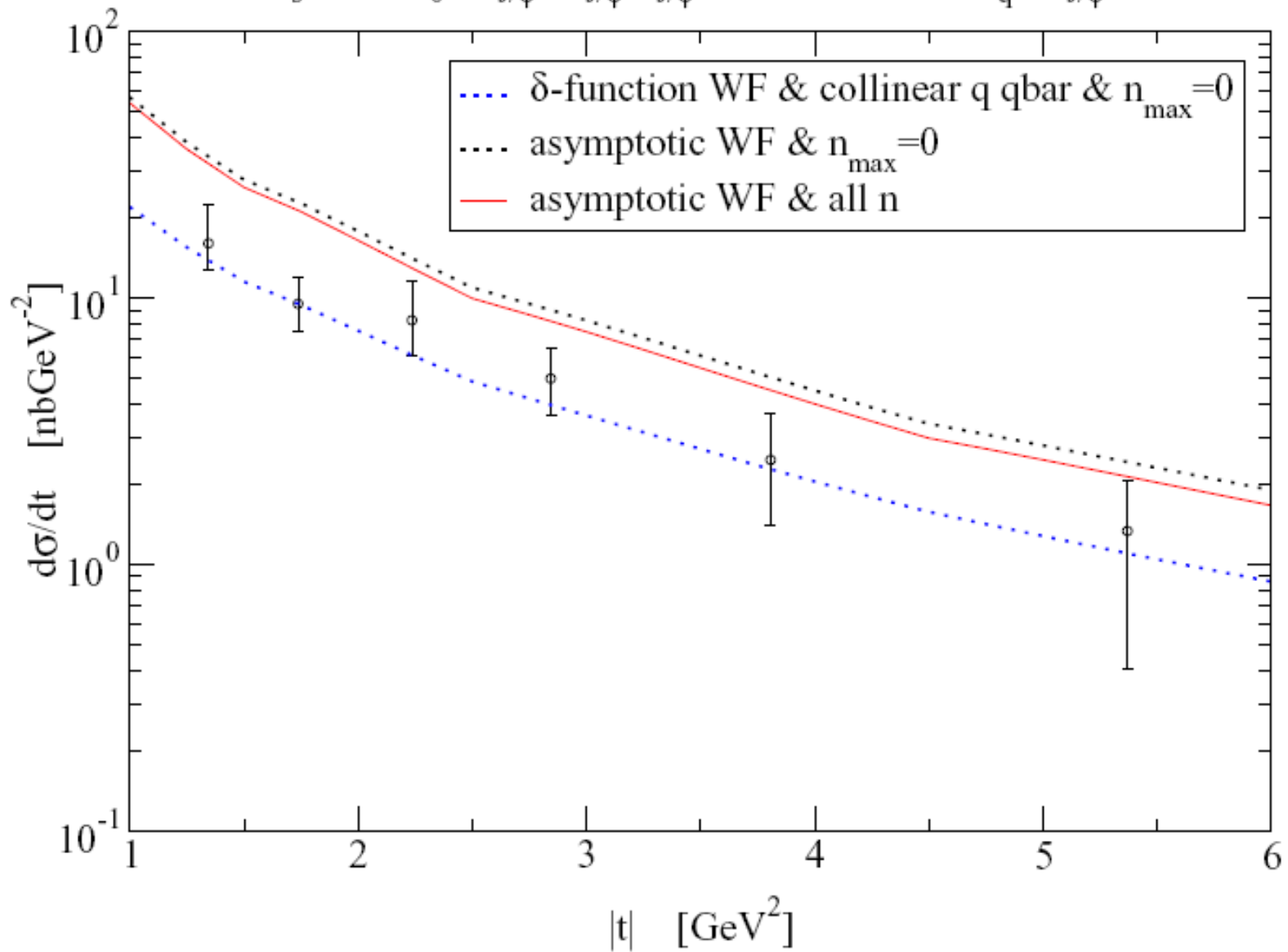
$$\alpha_s=0.20, s_0=m_\rho * m_\rho, f_\rho=0.217 \text{ GeV and } m_q=m_\rho/2$$



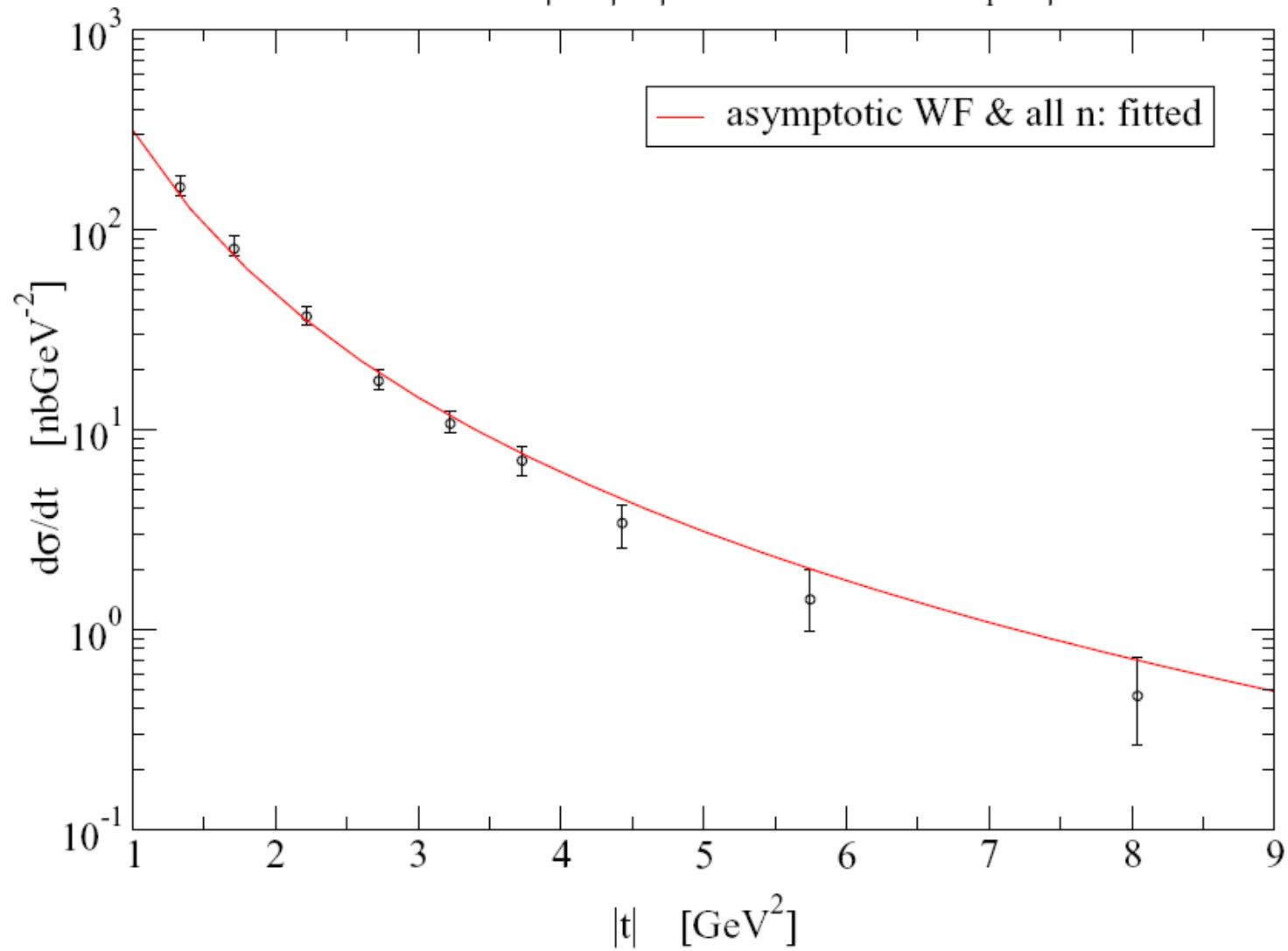
$\alpha_s=0.20, s_0=m_\phi*m_\phi, f_\phi=0.228 \text{ GeV}$  and  $m_q=m_\phi/2$



$$\alpha_s = 0.20, s_0 = m_{J/\psi} * m_{J/\psi}, f_{J/\psi} = 0.405 \text{ GeV and } m_q = m_{J/\psi}/2$$

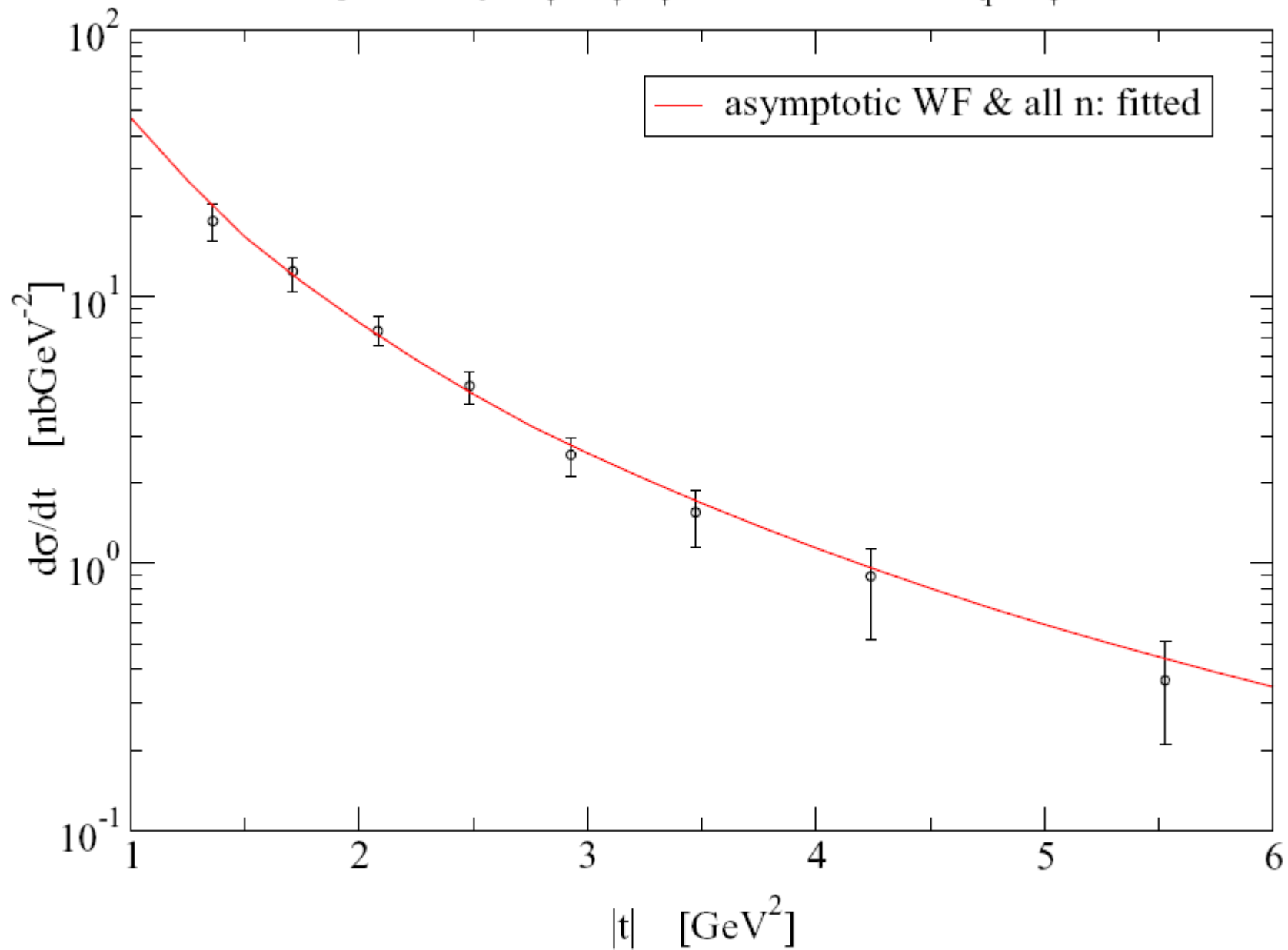


$$\alpha_s=0.18, s_0=m_\rho * m_\rho, f_\rho=0.217 \text{ GeV and } m_q=m_\rho/2$$

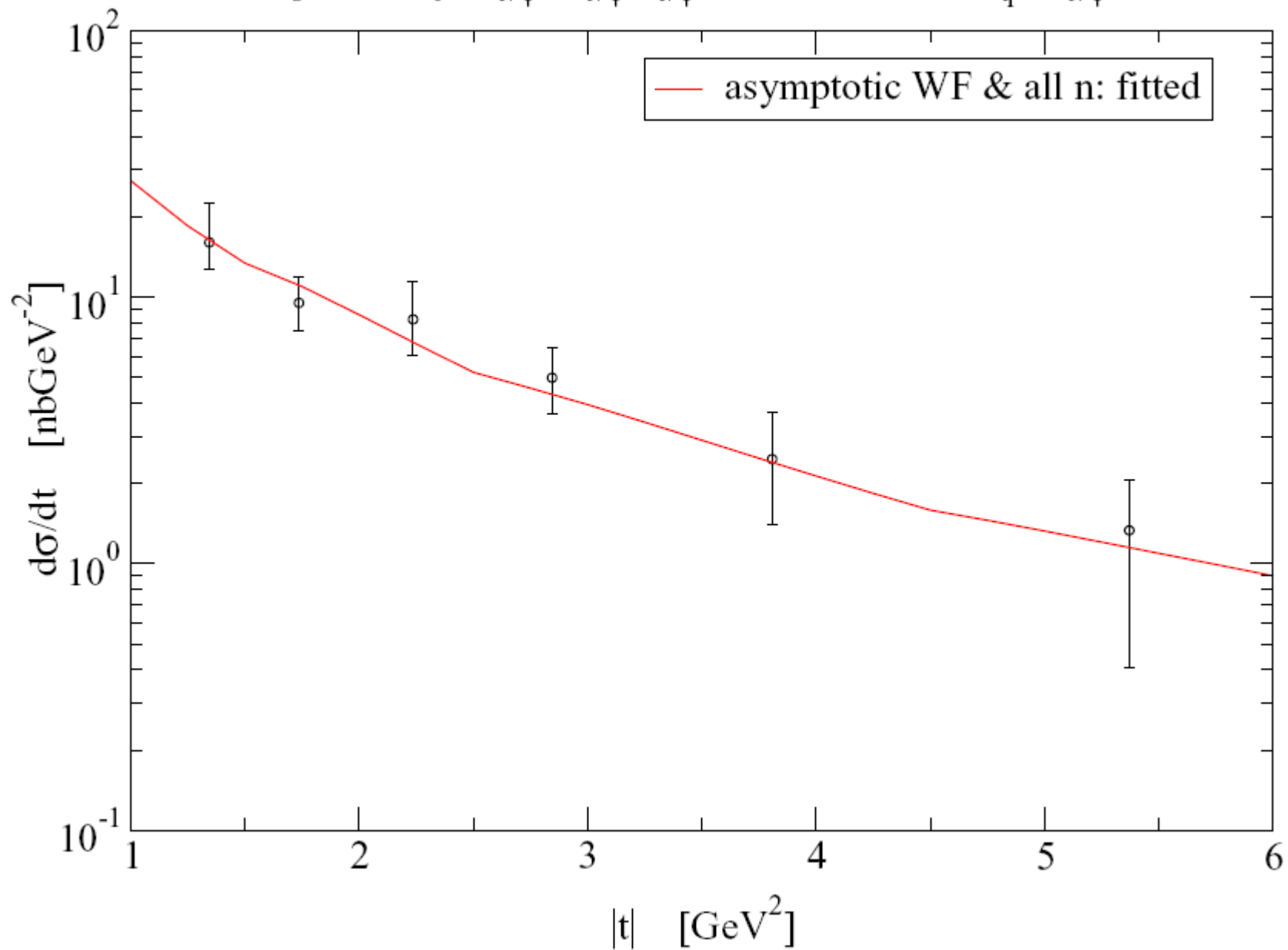




$\alpha_s=0.18, s_0=m_\phi * m_\phi, f_\phi=0.228 \text{ GeV}$  and  $m_q=m_\phi/2$

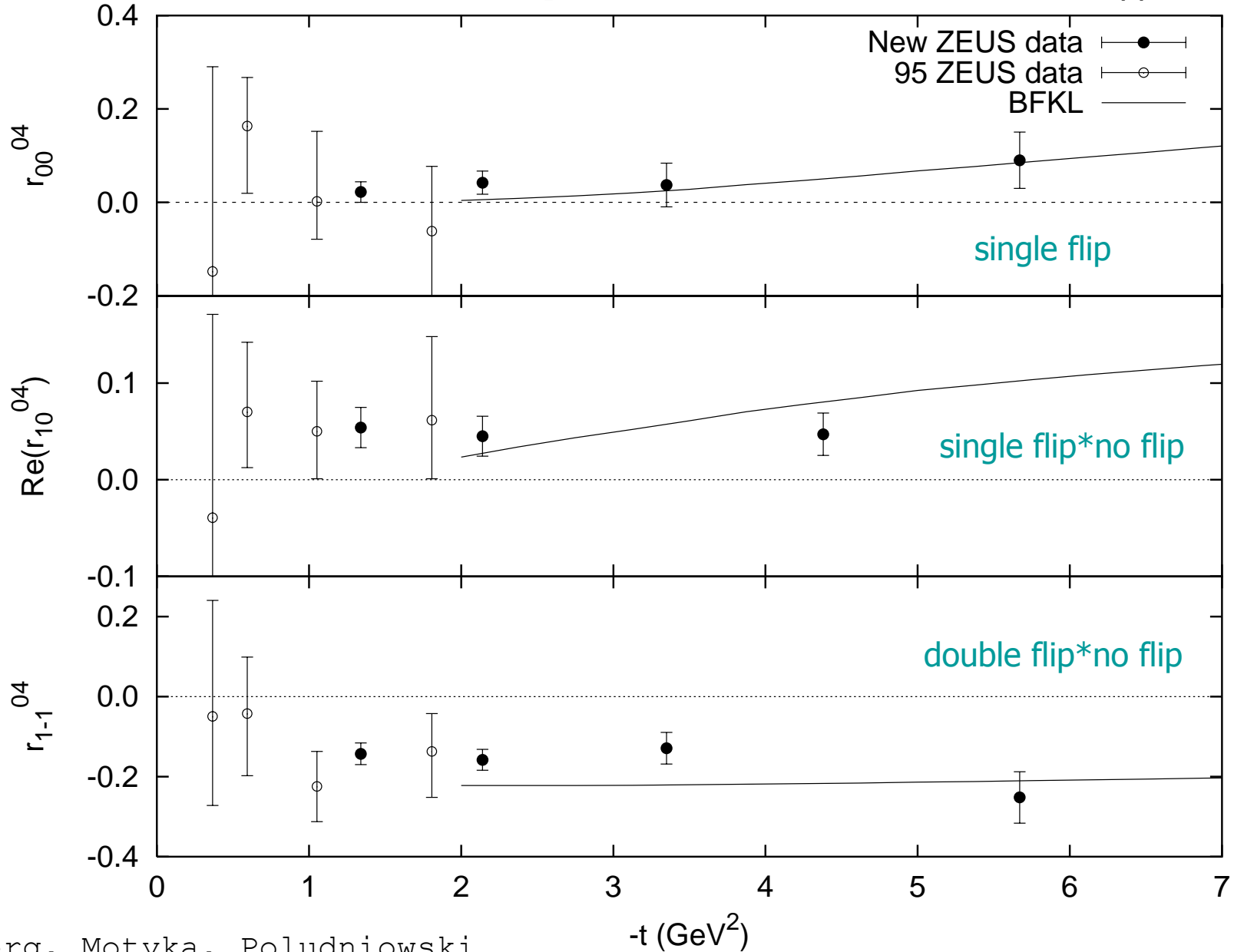


$$\alpha_s = 0.18, s_0 = m_{J/\psi} * m_{J/\psi}, f_{J/\psi} = 0.405 \text{ GeV and } m_q = m_{J/\psi} / 2$$



# Spin density matrix elements

[All these vanish in the non-relativistic approximation]



# Conclusions

- ✓ Vector meson production is proving an effective process in which to explore BFKL dynamics  
Two-gluon/fixed order exchange calculations do not do a good job
- ✓ Data require a large chiral odd contribution even for the rho meson can be generated in QCD either by using the constituent quark mass or by invoking the quark condensate – this explains in part the success of the “non-relativistic” model
- ✓ A full NLL calculation is desirable to get a handle on the normalization uncertainty and the treatment of the strong coupling
- ✓ Future:  $W$ -dependence, more accurate information on helicity structure (sensitive to meson wavefunctions), photons, omegas and upsilons.